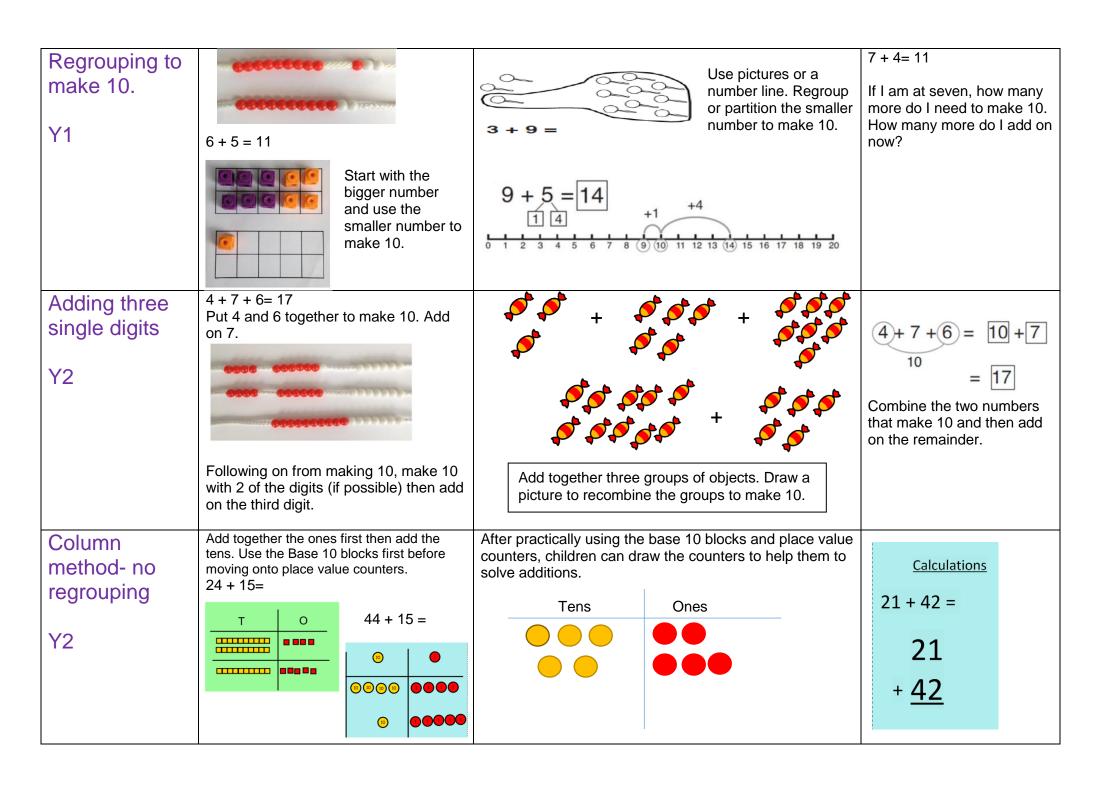
Calculations Guidance

This guidance has been written as a guide to indicate the progression through Addition, Subtraction, Multiplication and Division in Appleton Wiske School.

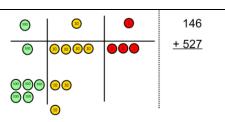
Addition

Objective and Strategies	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part-whole model Number bonds of 5,6,7,8,9 and 10 R/Y1	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7 3 + 4 = 7 10= 4 + 6 10= 6 + 4 5 Use the part-part whole diagram as shown above to move into the abstract.
Starting at the bigger number and counting	.0000000000	12 + 5 = 17	5 + 12 = 17
on Y1	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.



Column method- regrouping	Make both numbers on a place value grid. 49 + 23	Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.	Start by partitioning the numbers before moving on to clearly show the exchange below the addition.
Y2	Add up the units and exchange 10 ones for 1 ten. 10s 1s	35 + 27 = 62 Using tens and ones counters $30 + 20 = 50$ $5 + 7 = 12$ $50 + 12 = 62$	25 + 48 20 + 5 40 + 8 60 + 13 = 73
Column method- regrouping Y 3/4/5/6	Make both numbers on a place value grid.	Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding. NB Addition of money needs to have £ and p added separately.	$ \begin{array}{r} 536 \\ + 85 \\ \hline 621 \\ \hline 11 \end{array} $ As the children move on,

regrouping (continued) Y 3/4/5/6



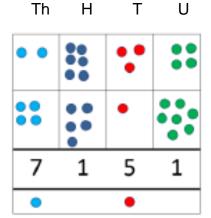
Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

Progress to adding 4 digit numbers and consolidate learning.





same number of decimal places and different. Money can be used here.

As the children progress, they will move from the expanded to the compacted method.

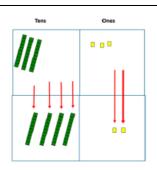
Subtraction

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones R/Y1	Use physical objects, counters, cubes etc to show how objects can be taken away. $6-2=4$ $4-2=2$	Cross out drawn objects to show what has been taken away.	18 -3= 15 8 - 2 = 6
Counting back Y1	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 – 4 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track $13-4=9$ 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. $57-23=34$ This can progress all the way to counting back using two 2 digit numbers.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help. 13 – 4 = 9

Find the	Compare amounts and objects to find		Hannah has 23 sandwiches,
	the difference.	*6 Count on to	Helen has 15 sandwiches.
difference	12 – 11 = 1	find the	Find the difference between
	1	difference.	the number of sandwiches.
Y1	Use cubes to	0 1 2 3 4 5 6 7 8 9 10 11 12	
	build towers or make bars to	11 – 6 = 5	23 – 15 = 8
	find the	11 0 = 0	20 10 = 0
	difference	Comparison Bar Models	
	5 Pencils		
	Use basic bar	Draw bars to Lisa is 13 years old. Her sister is 22 years old.	
	models with	find Find the difference in age between them. the difference	
	items to find the difference	between 2	
	3 Erasers 7	numbers.	
	, and the second	Sister	
	5 - 3 = 2	22 – 13 = 9	
		22	
Don't Don't	Link to addition- use	Use a pictorial representation of objects to show the part-	
Part-Part-	the part whole model	part-whole model. $6-2=4$	5
Whole Model	to help explain the	part whole medel.	3
	inverse between		10
Y1	addition and		
1 1	subtraction.		
	If 10 is the whole and 6 is one of the		Move to using numbers
	parts. What is the other part?	aims aims	within the part whole model.
	parto. What is the other part.		Within the part Whele medeli
	10 - 6 =		10 - 5 = 5
Make 10	14 – 9 =		
	99966 99666	13 - 7 = 6	16 – 8=
V4		34 -3	How many do we take off to
Y1		0 1 2 3 4 5 (6) 7 8 9 (10) 11 12 (13) 14 15 16 17 18 19 20	reach the next 10?
		Start at 13. Take away 3 to reach 10. Then take away the	TOGOTH THE HEALT TO:
	Make 14 on the ten frame. Take away the	remaining 4 so you have taken away 7 altogether. You	How many do we have left
	four first to make 10 and then takeaway one	have reached your answer.	to take off?
	more so you have taken away 5. You are	,	
	left with the answer of 9.		

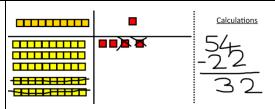
Column method without regrouping

Y2



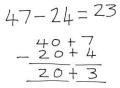
75-42=33

Use Base 10 to make the bigger number then take the smaller number away.

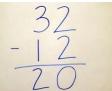


100	10	•	<u>Calculations</u>
100	<u>∞</u> 888 888	0000	176 - 64 = 176 - <u>64</u> 112

Draw the Base 10 or place value counters alongside the written calculation to help to show working.

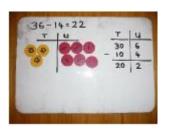


This will lead to a clear written column subtraction.



you partition numbers to subtract. Again make the larger number first.

Show how



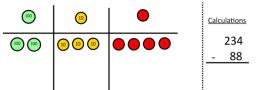
Column method with regrouping

Y3/4/5/6

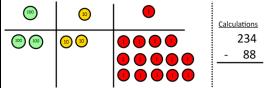
Column

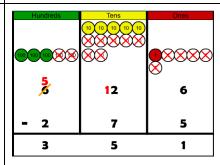
Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters



Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.





626 - 275 = 351

Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. Children can start their formal written method by partitioning the number into clear place value columns.





Moving forward the children use a more compact method.

This will lead to an understanding of

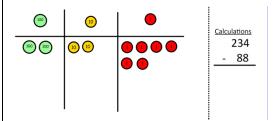
When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup.

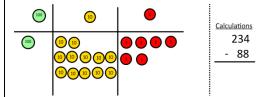
method with regrouping (continued)

Y3/4/5/6

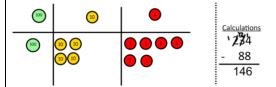
Now I can subtract my ones.



Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction



Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

subtracting any number including decimals.

Multiplication

Objective and Strategies	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number.	Draw pictures to show how to double a number.	16
R/Y1		Double 4 is 8	10 6 x2 x2
	double 4 is 8 4×2=8		Partition a number and then double each part before recombining it back together.
Counting in multiples		Sus our Sus our Sus our	Count in multiples of a number aloud. Write sequences with multiples of numbers.
R/Y1		0 5 10 15 20 25 30	2, 4, 6, 8, 10
		Use a number line or pictures to continue support in counting in multiples.	5, 10, 15, 20, 25 , 30
	Count in multiples supported by concrete objects in equal groups. 4 x 2 = 8	6 x 5 = 30	

Repeated addition

Y2







Use different objects to add equal groups.

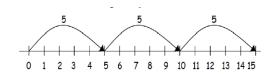
There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?







2 add 2 add 2 equals 6



5 + 5 + 5 = 15

 $3 \times 5 = 15$

Write addition sentences to describe objects and pictures.



5 x 2 = 10

Arraysshowing commutative multiplication

Y1/2/3/4

Create arrays using counters/ cubes to show multiplication sentences.



 $4 \times 6 = 24$



 $3 \times 5 = 15$

Draw arrays in different rotations to find **commutative** multiplication sentences.

 $4 \times 5 = 20$



Link arrays to area of rectangles.

0000 4×2=8

Use an array to write multiplication sentences and reinforce repeated addition.



$$5 + 5 + 5 = 15$$

$$3 + 3 + 3 + 3 + 3 = 15$$

$$5 \times 3 = 15$$

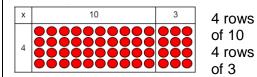
$$3 \times 5 = 15$$

Grid Method

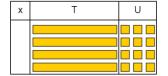
Y3/4/5/6

Show the link with arrays to first introduce the grid method.

$$13 \times 4 = 52$$

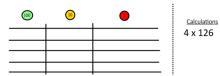


Move on to using Base 10 to move towards a more compact method.

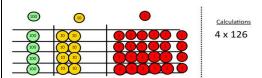


4 rows of 13

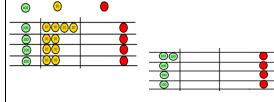
Move on to place value counters to show how we are finding groups of a number.We are multiplying by 4 so we need 4 rows.



Fill each row with 126.



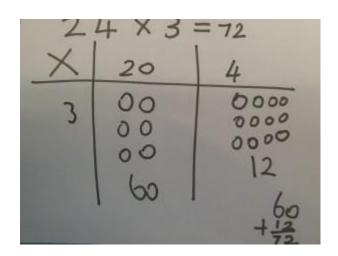
Add up each column, starting with the ones making any exchanges needed.



Then you have your answer.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.



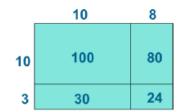
Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

$$18 \times 13 = 234$$



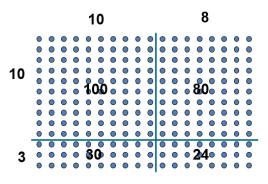
$$1342 \times 18 = 24,156$$

Х	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

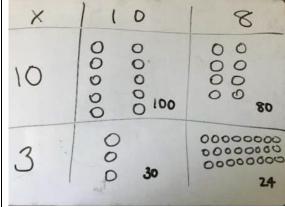
Column multiplication -Expanded method

Y3/4/5/6

Show the link with arrays to first introduce the expanded method.



$$18 \times 13 = 234$$

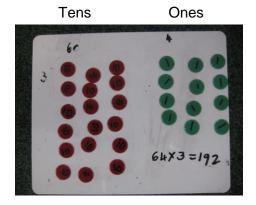


$$18 \times 13 = 234$$

Column
multiplication
-Compact
method

Y5/6

Children can continue to be supported by place value counters at the stage of multiplication.

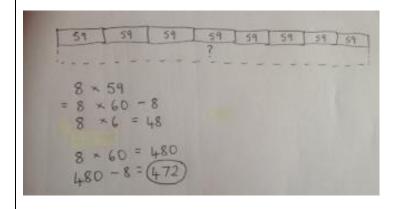


$$60 \times 3 = 180$$

$$4 \times 3 = 12$$

$$180 + 12 = 192$$

It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below. Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.



Start with long
multiplication, reminding
the children about lining up
their
numbers clearly in columns.

18

x <u>13</u>

24 (3 x 8)

30 (3 x 10))

80 (10 x 8)

100 (10 x 10)

234

1342

x 18 13420 10736

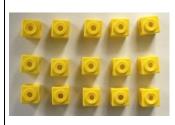
24156

Division

Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups R/Y1	10	Children use pictures or shapes to share quantities.	Share 9 buns between three people. $9 \div 3 = 3$
	I have 10 cubes, can you share them equally in 2 groups?	$8 \div 2 = 4$	
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups.	$28 \div 7 = 4$ Divide 29 into 7 groups
Y1/2	10 ÷ 5 = 2	0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 12÷3=4	Divide 28 into 7 groups. How many are in each group?
	35 ÷ 7 = 5 96 ÷ 3 = 32	Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	
		20 ? 20 ÷ 5 = ?	
		5 x ? = 20	

Division within arrays

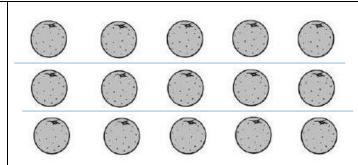
Y3/4/5/6



Link division to multiplication by creating an array and thinking about the

number sentences that can be created.

Eg
$$15 \div 3 = 5$$
 $5 \times 3 = 15$
 $15 \div 5 = 3$ $3 \times 5 = 15$



 $15 \div 3 = 5$

Draw an array and use lines to split the array into groups to make multiplication and division sentences.

Find the inverse of multiplication and division sentences by creating four linking number sentences.

$$7 \times 4 = 28$$

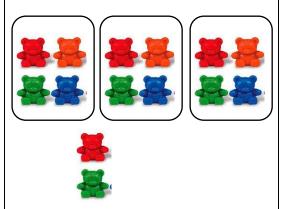
 $4 \times 7 = 28$
 $28 \div 7 = 4$
 $28 \div 4 = 7$

Division with a remainder

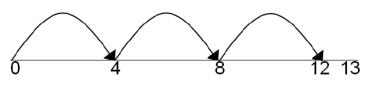
Y3/4/5/6

 $14 \div 3 = 4 r_2$

Divide objects between groups and see how much is left over



Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



 $13 \div 4 = 3 \text{ r } 1$

Draw dots and group them to divide an amount and clearly show a remainder.









 $14 \div 3 = 4 r 2$

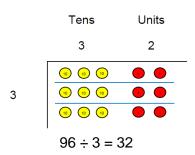
Complete written divisions and show the remainder using r.

$$29 \div 8 = 3 \text{ r } 5$$

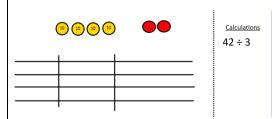
Long division		Children will use long
		division to divide numbers
		with up to 4 digits by 2 digit
		numbers.
Y3/4/5/6		
		015
		32 487
		-0
		48 -32 167
		22
		-32
		167
		-160
		7
		487 ÷ 32 = 15 r 7
		467 - 32 = 1517
		N9990 99902
		<u>17</u> r 19
		31 546 31 1 236
		311
		226
		236
		<u>217</u>
		19
		500 DEAD
		546 ÷ 31 = 17 r 19

Short division

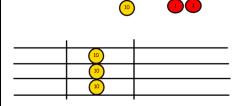
Y3/4/5/6



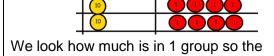
Use place value counters to divide using the bus stop method alongside $42 \div 3=$



Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

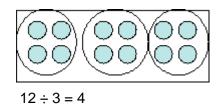


We exchange this ten for ten ones and then share the ones equally among the groups.

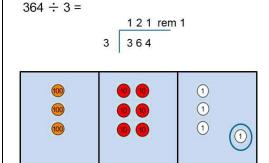


answer is 14.

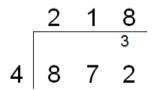
Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.



Begin with divisions that divide equally with no remainder.



Move onto divisions with a remainder.

Finally move into decimal places to divide the total accurately.